

Circle



1



$\frac{2}{2}$



$\frac{3}{3}$



$\frac{4}{4}$



$\frac{5}{5}$

Equivalences



$\frac{6}{6}$



$\frac{7}{7}$

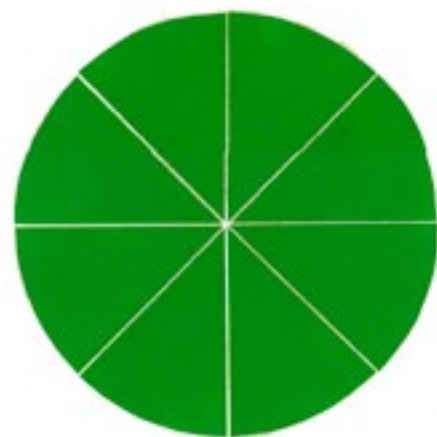


$\frac{2}{4}$

≡



$\frac{1}{2}$



$\frac{8}{8}$



$\frac{9}{9}$



$\frac{3}{6}$

≡



$\frac{1}{2}$



$\frac{4}{8}$

≡



$\frac{1}{2}$



$\frac{10}{10}$



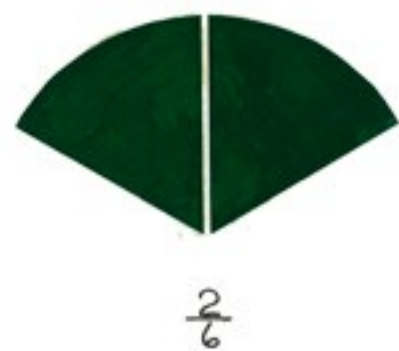
$\frac{5}{10}$

≡

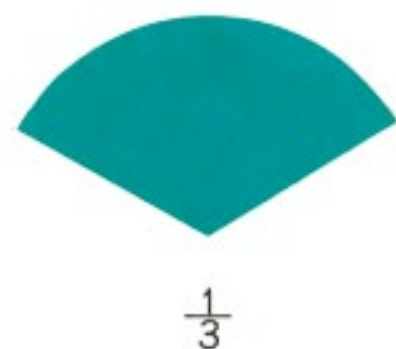


$\frac{1}{2}$

Equivalences



≡



≡



≡



≡



Addition

$$\frac{1}{5} + \frac{3}{5} =$$



$\frac{1}{5}$

+



$\frac{3}{5}$

=



$\frac{4}{5}$

$$\frac{1}{5} + \frac{3}{5} = \frac{4}{5}$$

Addition

$$\text{one half} = \frac{1}{2}$$



$\frac{1}{2}$

+



$\frac{1}{2}$



$\frac{2}{2}$

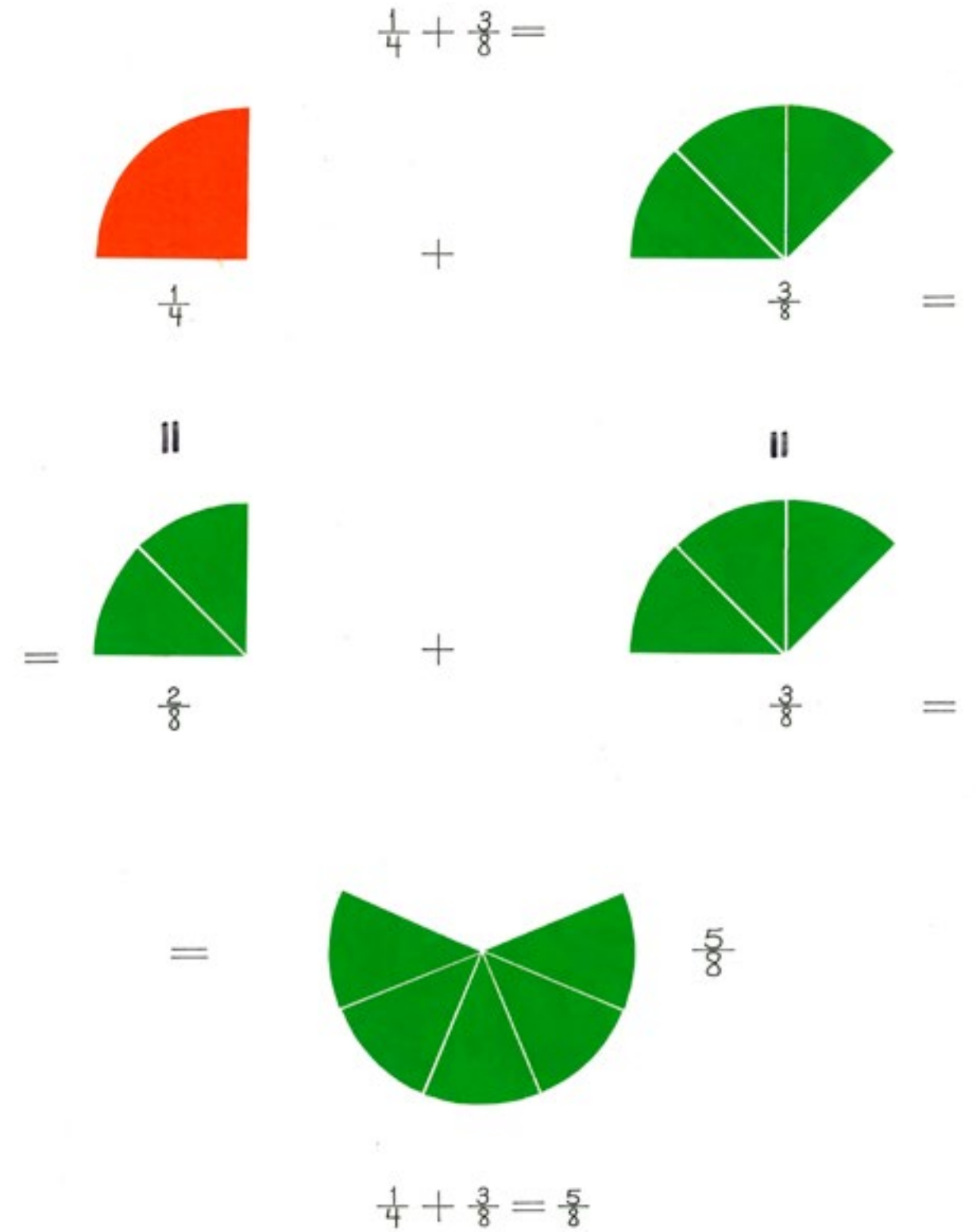
=



1

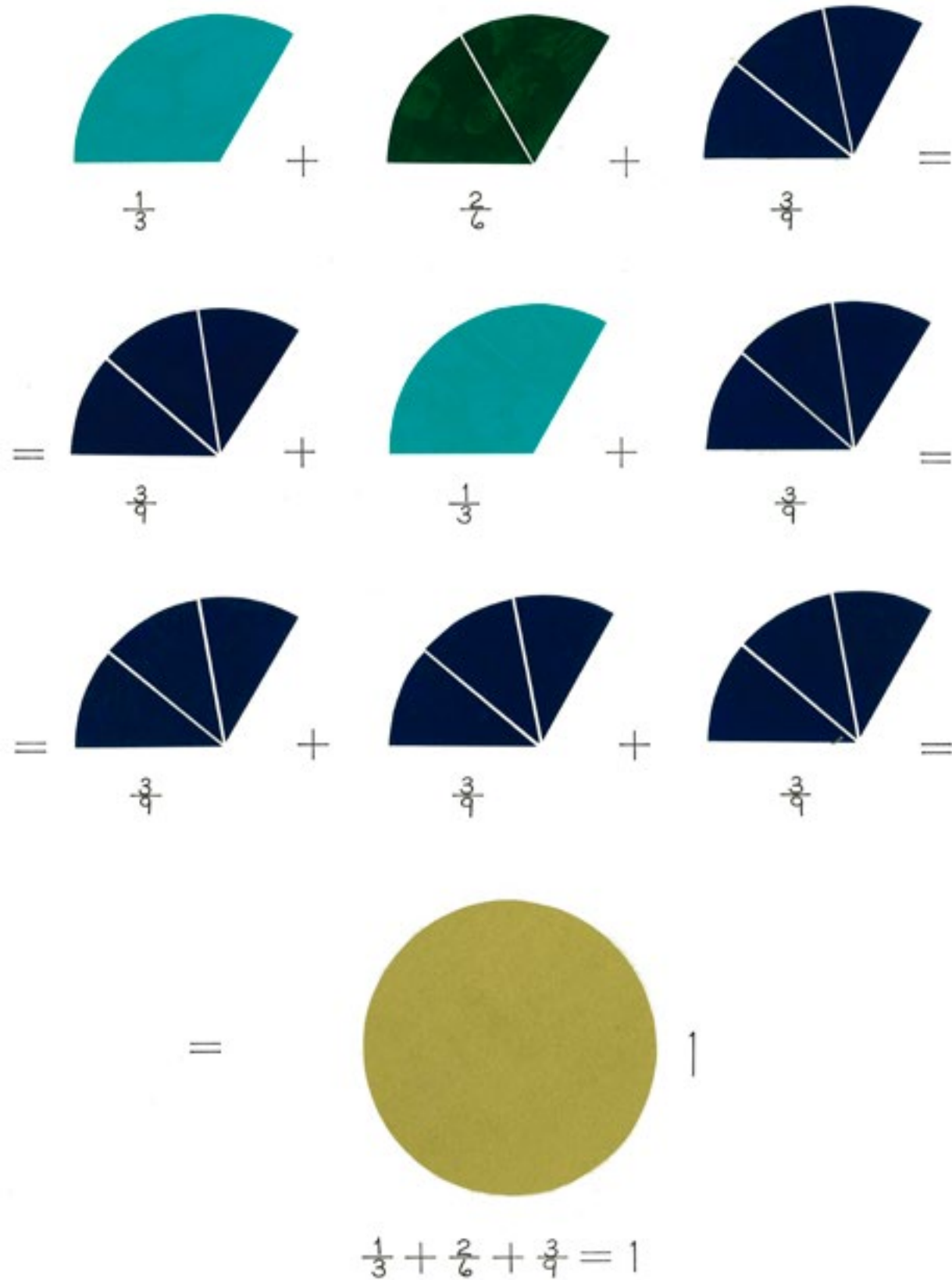
Addition

When fractions have the same denominator, the operations are carried out on the numerators. The result is given the same denominator as that of the fractions.



Addition

$$\frac{1}{3} + \frac{2}{6} + \frac{3}{9} =$$



If we multiply or divide the numerator and denominator of a fraction by the same number, the value remains the same.

For example: $\frac{2}{4} = \frac{1}{2}$;

if the numerator and denominator of the first fraction are both divided by 2, we obtain the second:

$$\frac{2 \div 2}{4 \div 2} = \frac{1}{2}$$

$$\frac{1}{2} = \frac{2}{4}$$

if the numerator and denominator of the first fraction are both multiplied by 2, we obtain the second:

$$\frac{1 \times 2}{2 \times 2} = \frac{2}{4}$$

If we multiply or divide the numerator and denominator of a fraction by the same number,

the value remains the same.

For example: $\frac{2}{4} = \frac{1}{2}$;

if the numerator and denominator of the first fraction are both divided by 2, we obtain the second:

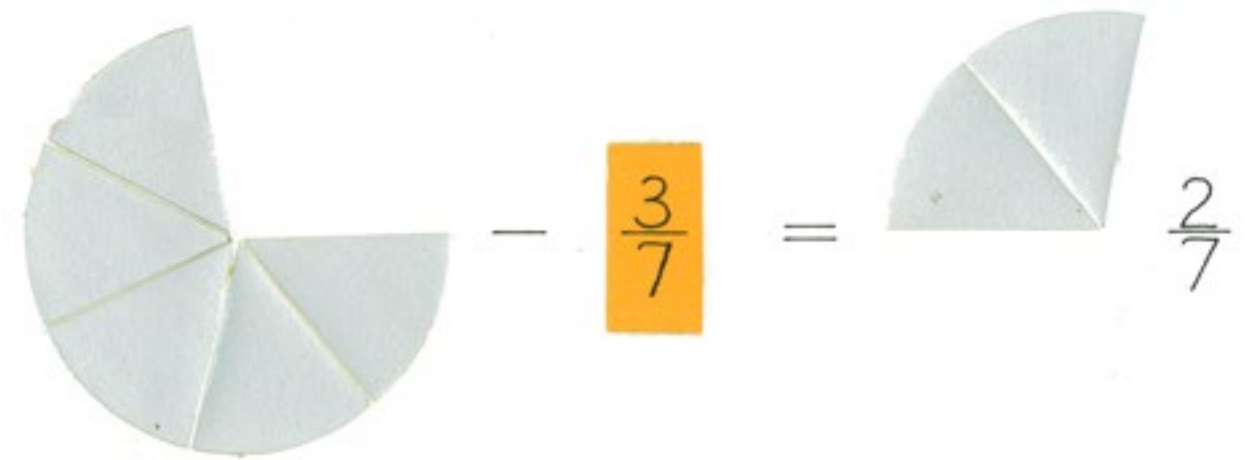
$$\frac{2 \div 2}{4 \div 2} = \frac{1}{2} \quad \frac{1}{2} = \frac{2}{4} ;$$

if the numerator and denominator of the first fraction are both multiplied by 2, we obtain the second:

$$\frac{1 \times 2}{2 \times 2} = \frac{2}{4}$$

Subtraction

$$\frac{5}{7} - \frac{3}{7} =$$



$$\frac{5}{7} - \frac{3}{7} = \frac{2}{7}$$

Subtraction

$$\frac{1}{2} - \frac{2}{10} =$$



$$- \frac{2}{10} =$$

=



$$- \frac{2}{10} =$$

=



$$\frac{3}{10} \quad \frac{1}{2} - \frac{2}{10} = \frac{3}{10}$$

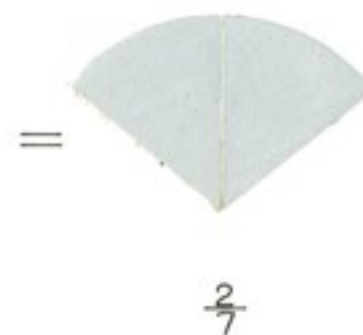
To subtract two fractions of different denominators, it is necessary first to change them to the same denominator, and then proceed with the operation.

Multiplication

$$\frac{2}{7} \times 3 =$$



$$\times 3 =$$



$\frac{2}{7}$



$\frac{2}{7}$



$\frac{2}{7}$

=

=



$\frac{6}{7}$

$$\frac{2}{7} \times 3 = \frac{6}{7}$$

Multiplication

multiplication means "to take"
to say $\frac{1}{3} \times 2$ means to take



to say $\frac{1}{3} \times \frac{1}{2}$ means to take



one half of the piece $\frac{1}{3}$.



Multiplication



$\frac{1}{4}$



\times

= the numerator is multiplied by 2.

$$\frac{1}{4} \times 2 = \frac{1 \times 2}{4} = \frac{2}{4}$$

$$\frac{1}{4} \times 2 = \frac{2}{4} = \frac{1}{2}$$



$\frac{2}{4}$

=



$\frac{1}{2}$



$\frac{1}{4}$



\times

= the denominator is divided by 2.

$$\frac{1}{4} \times 2 = \frac{1}{4 \div 2} = \frac{1}{2}$$



$\frac{1}{2}$

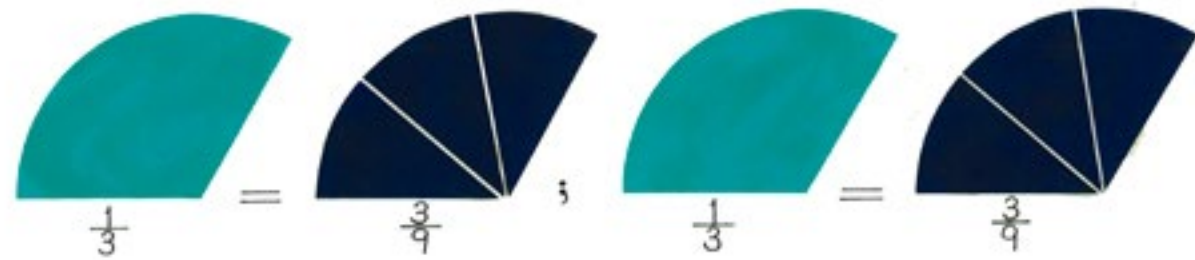
Rule: When multiplying a fraction by a whole, one can multiply the numerator by the whole number or, if divisible, divide the denominator by the whole number.

Multiplication

$$\frac{2}{3} \times \frac{2}{3} =$$



one must first divide each  in three parts



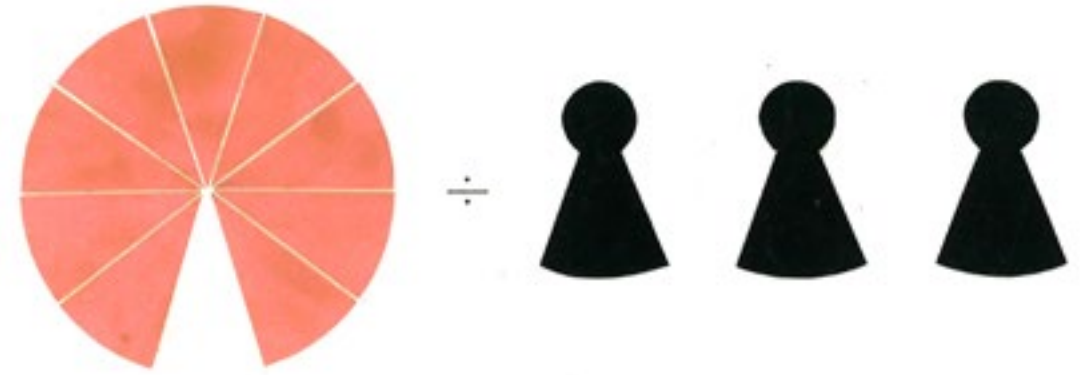
then take two parts of each third



Rule: To multiply a fraction by another fraction, one must multiply numerator by numerator and denominator by denominator.

Division

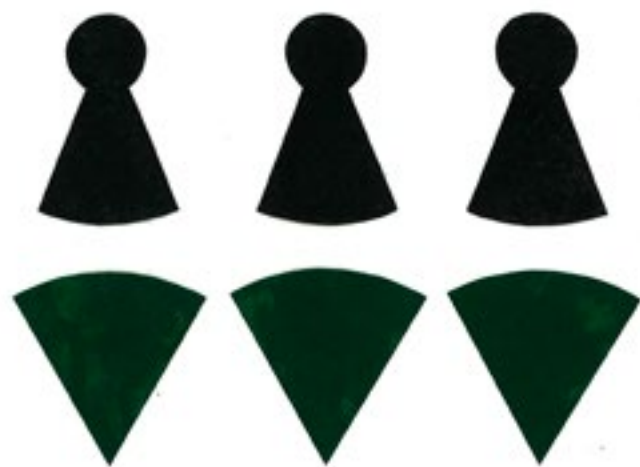
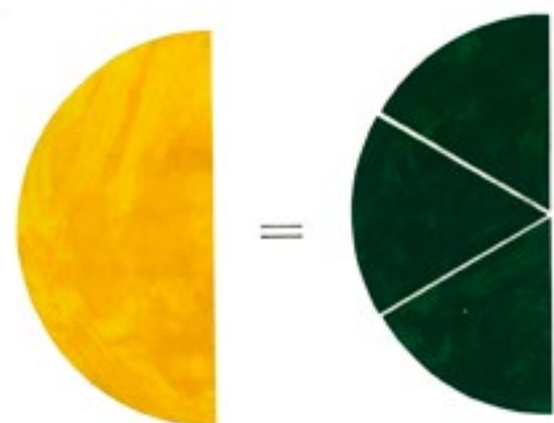
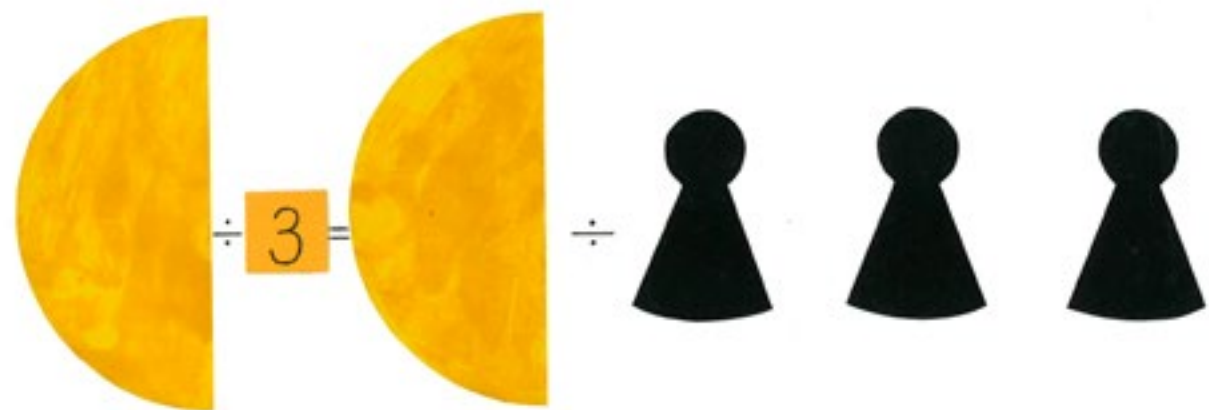
$$\frac{9}{10} \div 3 =$$



$$\frac{9}{10} \div 3 = \frac{3}{10}$$

Division

$$\frac{1}{2} \div 3 =$$

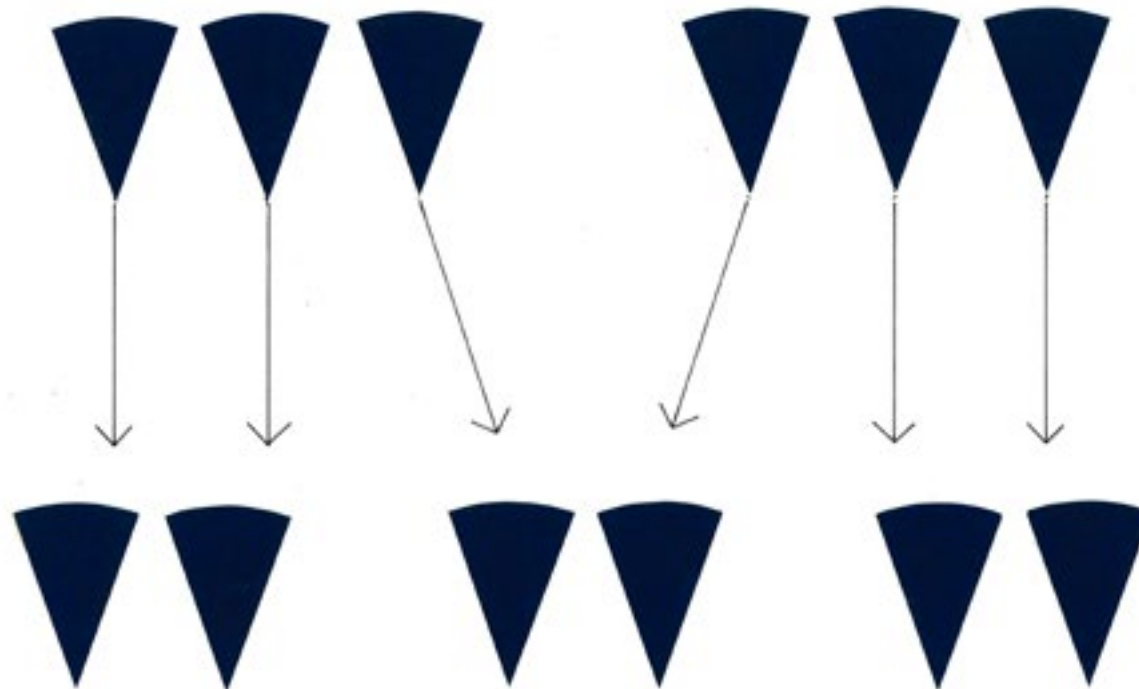


$$\frac{1}{2} \div 3 = \frac{1}{2 \times 3} = \frac{1}{6}$$

Rule: To divide a fraction by a whole number, instead of dividing the numerator, one can multiply the denominator by that number.

Group Division

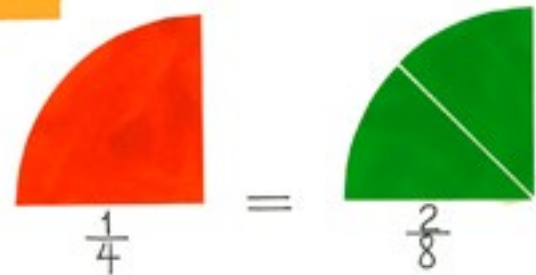
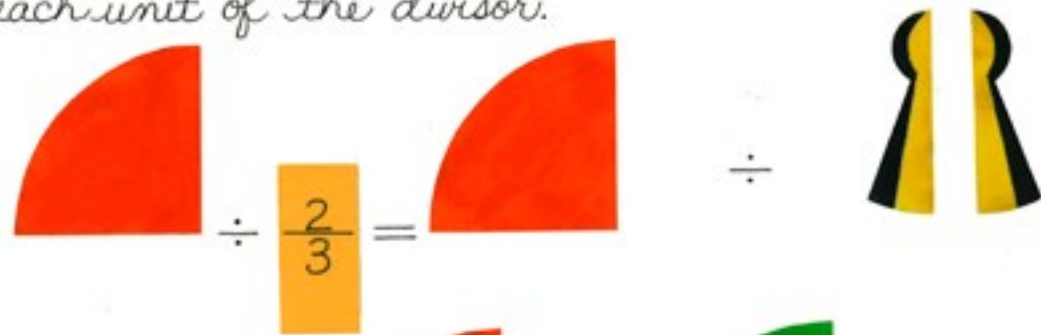
$\frac{2}{3} \div \frac{2}{9}$ = means to make with the $\frac{2}{9}$ as many groups of $\frac{2}{9}$ as possible.



$$\frac{2}{3} \div \frac{2}{9} = 3$$

So first the thirds must be divided into ninths. Then the ninths grouped into groups of two. When this is done, we find that we have three groups of $\frac{2}{9}$. 3 then is the result of the division.

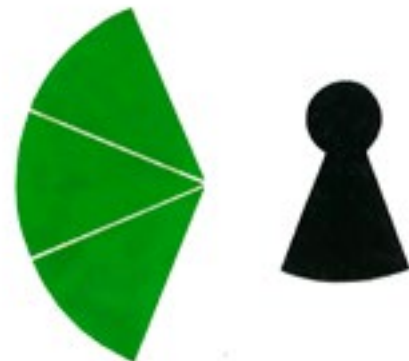
Division of fraction by fraction: in dividing a fraction by a fraction, one must remember that the result of the division is indicated by the amount received by each unit of the divisor.



each third will receive one half of $\frac{1}{4}$



As the unit is formed by 3 thirds, the result will be $\frac{3}{8}$.



Rule: To divide a fraction by a fraction, one multiplies the first by the inverse of the second.

$$\frac{1}{4} \div \frac{2}{3} = \frac{3}{8}$$